

Script generated by TTT

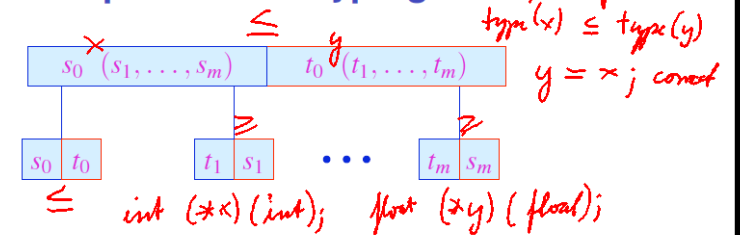
Title: Simon: Compilerbau (08.07.2013)

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Pages: 62

Rules and Examples for Subtyping



Examples:

$\text{struct } \{\text{int } a; \text{ int } b;\} \leq \text{struct } \{\text{float } a;\}$
 $\text{int } (\text{int}) \not\leq \text{float } (\text{float})$
 $\text{int } (\text{float}) \leq \text{float } (\text{int})$

Handwritten notes: $y = x; \text{ float } *y (\text{float}); \text{ float } r = *y (0.7)$

Attention:

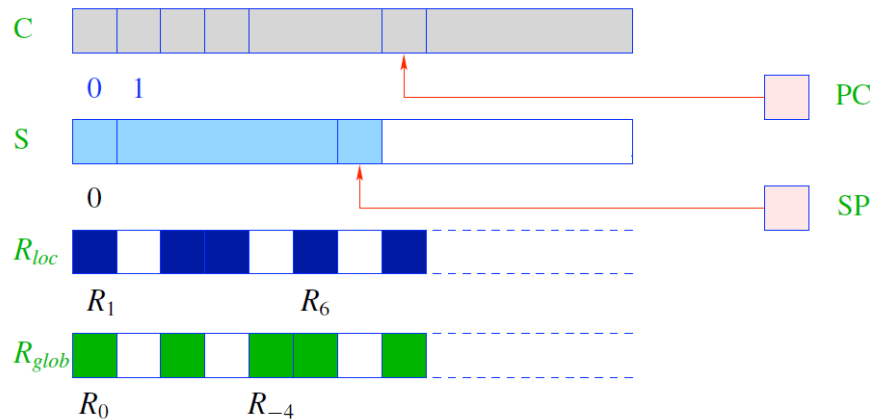
- For functions:
- the return types are in normal subtype relationship
- for argument types, the subtype relation reverses

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Principle of the Register C-Machine

The R-CMa is composed of a stack, heap and a code segment, just like the JVM; it additionally has register sets:

- *local* registers are $R_1, R_2, \dots, R_i, \dots$
- *global* registers are $R_0, R_{-1}, \dots, R_j, \dots$



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The Register Sets of the R-CMa

The two register sets have the following purpose:

- 1 the *local* registers R_i
 - save temporary results
 - store the contents of local variables of a function
 - can efficiently be stored and restored from the stack
- 2 the *global* registers R_i
 - save the parameters of a function
 - store the result of a function

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Translation of Simple Expressions

Using variables stored in registers; loading constants:

instruction	semantics	intuition
loadc R_i c	$R_i = c$	load constant
move R_i R_j	$R_i = R_j$	copy R_j to R_i

We define the following translation schema (with $\rho x = a$):

$\text{code}_R^i c \rho$	=	loadc R_i c
$\text{code}_R^i x \rho$	=	move R_i R_a
$\text{code}_R^i x = e \rho$	=	$\text{code}_R^i e \rho$ move R_a R_i

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$\text{code}_R^i x = e \rho$	=	$\text{code}_R^i e \rho$ move R_a R_i

Note: all instructions use the Intel convention (in contrast to the AT&T convention): $\text{op } \text{dst } \text{src}_1 \dots \text{src}_n$.

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Translation of Expressions

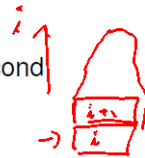
Let $\text{op} = \{\text{add}, \text{sub}, \text{div}, \text{mul}, \text{mod}, \text{le}, \text{gr}, \text{eq}, \text{leq}, \text{geq}, \text{and}, \text{or}\}$. The R-CMa provides an instruction for each operator op .

$\text{op } R_i R_j R_k$

where R_i is the target register, R_j the first and R_k the second argument.

Correspondingly, we generate code as follows:

$\text{code}_R^i e_1 \text{op } e_2 \rho$	=	$\text{code}_R^i e_1 \rho$ $\text{code}_R^{i+1} e_2 \rho$ $\text{op } R_i R_i R_{i+1}$
---	---	--



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Translation of Expressions

Let $\text{op} = \{\text{add}, \text{sub}, \text{div}, \text{mul}, \text{mod}, \text{le}, \text{gr}, \text{eq}, \text{leq}, \text{geq}, \text{and}, \text{or}\}$. The R-CMa provides an instruction for each operator op .

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---	---	--

Example: Translate $3 * 4$ with $i = 4$:

$\text{code}_R^4 3 * 4 \rho$	=	$\text{code}_R^4 3 \rho$ $\text{code}_R^5 4 \rho$ $\text{mul } R_4 R_4 R_5$
------------------------------	---	---

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Applying Translation Schema for Expressions

Suppose the following function is given:

```
void f(void) {
    int x, y, z;
    x = y+z*3;
}
```

- Let $\rho = \{x \mapsto 1, y \mapsto 2, z \mapsto 3\}$ be the address environment.
- Let R_4 be the first free register, that is, $i = 4$.

$code^4_{x=y+z*3} \rho = code^4_{y+z*3} \rho = move_{R_1 R_4} \quad \text{if } (1, 2)$
 $code^4_{y+z*3} \rho = move_{R_4 R_2} \quad \text{if } (2, 3)$
 $code^5_{z*3} \rho = add_{R_4 R_4 R_5} \quad \text{if } (3)$

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About Statements and Expressions

General idea for translation:

$code^i s \rho$: generate code for statement s
 $code^i_R e \rho$: generate code for expression e into R_i

Throughout: $i, i+1, \dots$ are free (unused) registers

For an *expression* $x = e$ with $\rho.x = a$ we defined:

$code^i_R x = e \rho = code^i_R e \rho$
 $move_{R_a R_i}$

However, $x = e$ is also a *statement*:

- Define:

$code^i_{e_1 = e_2} \rho = code^i_{e_1 = e_2} \rho$

The temporary register R_i is ignored here. More general:

$code^i e \rho = code^i e \rho$

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$code^i e \rho = code^i e \rho$

- Observation:** the assignment to e_1 is a side effect of the evaluating the expression $e_1 = e_2$.

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Translation of Statement Sequences

The code for a sequence of statements is the concatenation of the instructions for each statement in that sequence:

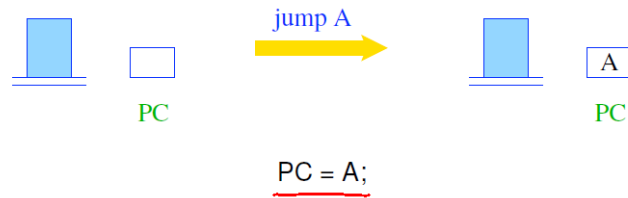
$code^i (s; ss) \rho = code^i s \rho$
 $code^i_{\epsilon} \rho = // \text{ empty sequence of instructions}$

Note here: s is a statement, ss is a sequence of statements

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Jumps

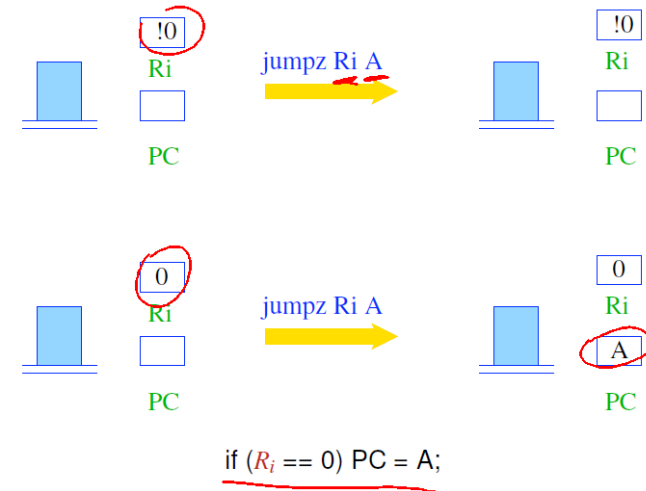
In order to diverge from the linear sequence of execution, we need *jumps*:



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Conditional Jumps

A conditional jump branches depending on the value in R_i :



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Management of Control Flow

In order to translate statements with control flow, we need to emit jump instructions.

- during the translation of an **if** (c) construct, it is not yet clear where to jump to in case that c is false

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- during the translation of an **if** (c) construct, it is not yet clear where to jump to in case that c is false
- instruction sequences may be arranged in a different order
 - minimize the number of *unconditional* jumps
 - minimize in a way so that fewer jumps are executed inside loops
 - replace far jumps through near jumps (if applicable)

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- organize instruction sequence into blocks without jumps

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- instruction sequences may be arranged in a different order
 - minimize the number of *unconditional* jumps
 - minimize in a way so that fewer jumps are executed inside loops
 - replace *far jumps* through *near jumps* (if applicable)
- organize instruction sequence into blocks without jumps

To this end, we define:

Definition

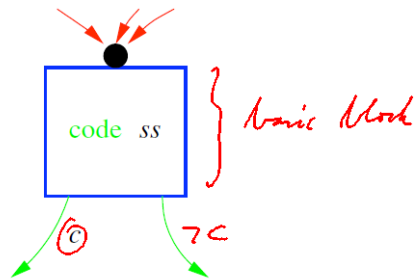
A basic block consists of

- a sequence of statements ss that does not contain a jump
- a set of outgoing edges to other basic blocks
- where each edge may be labelled with a condition

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Basic Blocks and the Register C-Machine

The **R-CMa** features only a single conditional jump, namely jumpz.

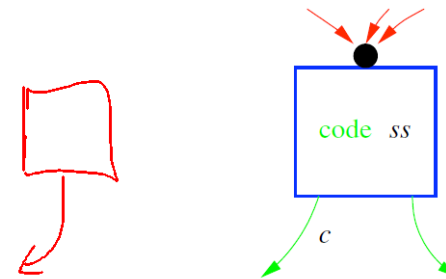


Outgoing edges must have the following form:

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Basic Blocks and the Register C-Machine

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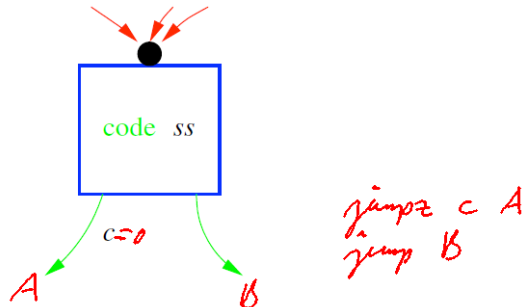
Outgoing edges must have the following form:

- a single edge (unconditional jump), translated with **jump**

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Basic Blocks and the Register C-Machine

The R-CMa features only a single conditional jump, namely `jumpz`.



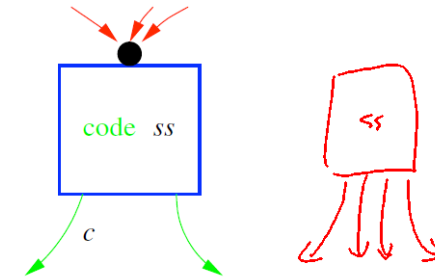
Outgoing edges must have the following form:

- 1 a single edge (unconditional jump), translated with `jump`
- 2 two edges, one with `c = 0` as condition and one without condition, translated with `jumpz` and `jump`, respectively

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Basic Blocks and the Register C-Machine

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Outgoing edges must have the following form:

- 1 a single edge (unconditional jump), translated with `jump`
- 2 two edges, one with `c = 0` as condition and one without condition, translated with `jumpz` and `jump`, respectively
- 3 a set of edges and one `default` edge, used for `switch` statement, translated with `jumpi` and `jump` (to be discussed later)

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Formalizing the Translation Involving Control Flow

For simplicity of defining translations of instructions involving control flow, we use symbolic jump targets.

- This translation can be used in practice, but a second run through the emitted instructions is necessary to resolve the symbolic addresses to actual addresses.

jump A
⋮
A: mov

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For simplicity of defining translations of instructions involving control flow, we use symbolic jump targets.

- This translation can be used in practice, but a second run through the emitted instructions is necessary to resolve the symbolic addresses to actual addresses.

Alternatively, we can emit relative jumps without a second pass:

- relative jumps have targets that are offsets to the current PC
- sometime relative jumps only possible for small offsets (\leadsto near jumps)
- if all jumps are relative: the code becomes position independent (PIC), that is, it can be moved to a different address
- the generated code can be loaded without relocating absolute jumps

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Formalizing the Translation Involving Control Flow

For simplicity of defining translations of instructions involving control flow, we use *symbolic jump targets*.

- This translation can be used in practice, but a second run through the emitted instructions is necessary to *resolve* the symbolic addresses to actual addresses.

Alternatively, we can emit *relative* jumps without a second pass:

- relative jumps have targets that are offsets to the current PC
- sometime relative jumps only possible for small offsets (\sim near jumps)
- if all jumps are relative: the code becomes *position independent* (PIC), that is, it can be moved to a different address
- the generated code can be loaded without relocating absolute jumps

generating a graph of *basic blocks* is useful for *program optimization* where the statements inside basic blocks are simplified

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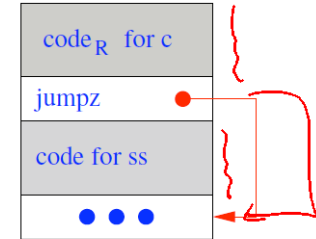
Simple Conditional

We first consider $s \equiv \text{if } (c) \{ ss \}$...and present a translation without basic blocks.

Idea:

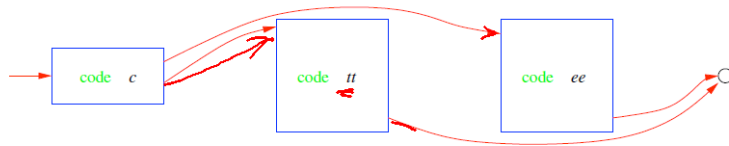
- emit the code of c and ss in sequence
- insert a jump instruction in-between, so that correct control flow is ensured

$$\text{code}_R^i s \rho = \begin{array}{l} \text{code}_R^i c \rho \\ \text{jumpz } R_i A \\ \text{code}_R^i ss \rho \\ A: \dots \end{array}$$



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General Conditional



Translation of $\text{if } (c) \text{ tt else } ee.$

$$\text{code}_R^i \text{if}(c) \text{ tt else } ee \rho = \begin{array}{l} \text{code}_R^i c \rho \\ \text{jumpz } R_i A \\ \text{code}_R^i tt \rho \\ \text{jump } B \\ A: \text{code}_R^i ee \rho \\ B: \end{array}$$

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Example for if-statement

Let $\rho = \{x \mapsto 4, y \mapsto 7\}$ and let s be the statement $x = 8$

```

if (x > y) {           /* (i) */
  x = x - y;          /* (ii) */
} else {
  y = y - x;          /* (iii) */
}
    
```

Then $\text{code}_R^i s \rho$ yields:

$\text{code}_R^i x > y \rho = \text{mov } R_8 R_4$
 $\text{mov } R_9 R_7$
 $\text{gt } R_8 R_9$
 $\text{jumpz } R_8 A$
 $\text{code}_R^i x = x - y \rho$
 $A: \text{jump } B$
 $\text{code}_R^i y = y - x \rho$
 $B:$

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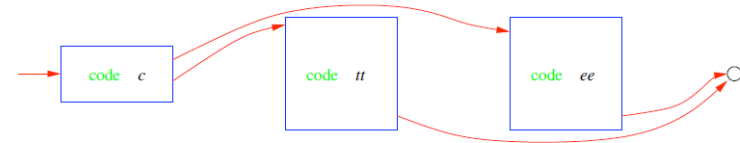
if (x>y) {      /* (i) */
  x = x - y;     /* (ii) */
} else {
  y = y - x;     /* (iii) */
}
    
```

Then $\text{code}^i s \rho$ yields:

```

(i)      (ii)      (iii)
move Ri R4      move R7 R4      move R7 R7
move Ri+1 R7    move Ri+1 R7      move Ri+1 R4
gr Ri Ri Ri+1  sub Ri Ri Ri+1  sub Ri Ri Ri+1
jumpz Ri A      move R4 Ri      move R7 Ri
                        jump B
    
```

General Conditional

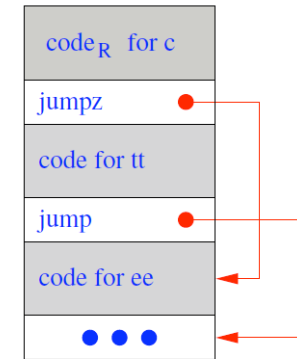


Translation of **if** (c) tt **else** ee .

$\text{code}^i \text{if}(c) tt \text{ else } ee \rho =$

```

codeR c ρ
jumpz Ri A
codeR tt ρ
jump B
A : codeR ee ρ
B :
    
```



Iterating Statements

We only consider the loop $s \equiv \text{while } (e) s$. For this statement we define:

$\text{code}^i \text{while}(e) s \rho =$

```

A : codeR e ρ
  jumpz Ri B
  codeR s ρ
  jump A
B :
    
```

$\text{code}^i \text{while}(e) s \rho = \text{jump A}$
 $C_i \text{code}^i s \rho$

A : code_R e ρ
 jump B R_i B
 v : jump C

Example: Translation of Loops

Let $\rho = \{a \mapsto 7, b \mapsto 8, c \mapsto 9\}$ and let s be the statement:

```

while (a>0) { /* (i) */
  c = c + 1;    /* (ii) */
  a = a - b;    /* (iii) */
}
    
```

Then $\text{code}^i s \rho$ evaluates to:

```

(i) A : move Ri R7
      loadc Ri+1 0
      gr Ri Ri Ri+1
      jumpz Ri B

(ii)      move Ri R9
          loadc Ri+1 1
          add Ri Ri Ri+1
          move R9 Ri

(iii)     move Ri R7
          move Ri+1 R8
          sub Ri Ri Ri+1
          move R7 Ri
          jump A
B :
    
```


for-Loops

The **for**-loop $s \equiv \mathbf{for} (e_1; e_2; e_3) s'$ is equivalent to the statement sequence e_1 ; **while** (e_2) $\{s' e_3\}$ – as long as s' does not contain a **continue** statement.

Thus, we translate:

```

codei for(e1; e2; e3) s' ρ = codeiR(e1) ρ
                                A: codeiR(e2) ρ
                                jumpz R(B)
                                codei s' ρ
                                codei(e3) ρ
                                jump A
                                B:
    
```

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The switch-Statement

Idea:

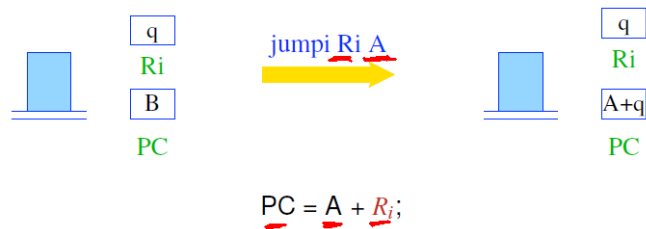
- Suppose choosing from multiple options in constant time if possible
- use a jump table that, at the i th position, holds a jump to the i th alternative
- in order to realize this idea, we need an indirect jump instruction

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The switch-Statement

Idea:

- Suppose choosing from multiple options in constant time if possible
- use a jump table that, at the i th position, holds a jump to the i th alternative
- in order to realize this idea, we need an indirect jump instruction



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Consecutive Alternatives

Let **switch** s be given with k consecutive **case** alternatives:

```

switch (e) {
  case c0 s0; break;
  :
  case ck-1 sk-1; break;
  default: s; break;
}
    
```

that is, $c_i + 1 = c_{i+1}$ for $i = [0, k - 1]$.

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Consecutive Alternatives

Let `switch s` be given with k consecutive `case` alternatives:

```
switch (e) {
  case  $c_0$ :  $s_0$ ; break;
  :
  case  $c_{k-1}$ :  $s_{k-1}$ ; break;
  default:  $s$ ; break;
}
```

that is, $c_i + 1 = c_{i+1}$ for $i = [0, k - 1]$.

Define `codei s ρ` as follows:

```
codei s ρ = codeiR e ρ
             checki  $c_0$   $c_{k-1}$   $B$   $C$ 
A0: codei  $s_0$  ρ      (B): jump A0
      jump D           :
                       :
                       :      jump Ak-1
Ak-1: codei  $s_{k-1}$  ρ
      jump D           C: code s ρ } default
                       0:
```

Handwritten notes: $B+R_i$ (with arrow from B to C), $C: code s \rho$ }

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  :
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}
```

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Define `codei s ρ` as follows:

```
codei s ρ = codeiR e ρ
             checki  $c_0$   $c_{k-1}$   $B$ 
A0: codei  $s_0$  ρ      B: jump A0
      jump D           :
                       :
                       :      jump Ak-1
Ak-1: codei  $s_{k-1}$  ρ
      jump D           C:
                       checki  $l$   $u$   $B$  checks if  $l \leq R_i \leq u$  holds and jumps accordingly.
```

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Translation of the `checki` Macro

The macro `checki l u B` checks if $l \leq R_i < u$. Let $k = u - l$.

- if $l \leq R_i < u$ it jumps to $B + R_i - l$
- if $R_i < l$ or $R_i \geq u$ it jumps to C

```
B: jump A0
:
:      jump Ak-1
C:
```

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we define: $R_i - l \geq k$

```
checki l u B = loadc  $R_{i+1}$   $l$ 
                geq  $R_{i+2}$   $R_i$   $R_{i+1}$ 
                jumpz  $R_{i+2}$   $E$ 
                sub  $R_i$   $R_i$   $R_{i+1}$ 
                loadc  $R_{i+1}$   $k$ 
                geq  $R_{i+2}$   $R_i$   $R_{i+1}$ 
                jumpz  $R_{i+2}$   $D$ 
                E: loadc  $R_i$   $k$ 
                D: jumpi  $R_i$   $B$ 
                B: jump A0
                :
                :      jump Ak-1
                C:
                 $R_i - l$ 
```

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- if $R_i < l$ or $R_i \geq u$ it jumps to C

we define:

```

 $check^i l u B$  =   loadc  $R_{i+1} l$ 
                   geq  $R_{i+2} R_i R_{i+1}$ 
                   jumpz  $R_{i+2} E$ 
                   sub  $R_i R_i R_{i+1}$ 
                   loadc  $R_{i+1} k$ 
                   geq  $R_{i+2} R_i R_{i+1}$ 
                   jumpz  $R_{i+2} D$ 
E:   loadc  $R_i k$ 
D:   jumpi  $R_i B$ 

B:   jump  $A_0$ 
      ⋮
      ⋮
      jump  $A_{k-1}$ 
C:

```

Note: a jump $jumpi R_i B$ with $R_i = k$ winds up at C .

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Improvements for Jump Tables

This translation is only suitable for *certain* **switch**-statement.

- In case the table starts with 0 instead of Q we don't need to subtract it from e before we use it as index
- if the value of e is guaranteed to be in the interval $[l, u]$, we can omit check
- can we implement the **switch**-statement using an L -attributed system without symbolic labels?

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- In case the table starts with 0 instead of u we don't need to subtract it from e before we use it as index
- if the value of e is guaranteed to be in the interval $[l, u]$, we can omit check
- can we implement the **switch**-statement using an L -attributed system without symbolic labels?
 - difficult since B is unknown when $check^i$ is translated
 - \leadsto use symbolic labels or basic blocks

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General translation of switch-Statements

In general, the values of the various cases may be far apart:

- generate an **if**-ladder, that is, a sequence of **if**-statements

Handwritten notes illustrating an if-ladder for a switch statement:

```

switch (a) {
case 5:
    ...
}

if (a == 12) {
    ...
} else if (a == 9) {
    ...
} else if (a == 5) {
    ...
} else if (a == 7) {
    ...
} else if (a == 12) {
    ...
} else {
    ...
}

```

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General translation of switch-Statements

In general, the values of the various cases may be far apart:

- generate an **if**-ladder, that is, a sequence of **if**-statements
- for n cases, an **if**-cascade (tree of conditionals) can be generated $\sim O(\log n)$ tests

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- one could generate several jump tables, one for each sets of consecutive cases
- an **if** cascade can be re-arranged by using information from *profiling*, so that paths executed more frequently require fewer tests

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Translation into Basic Blocks

Problem: How do we connect the different basic blocks?

Idea:

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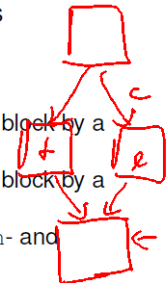
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- similar for other constructs

For better navigation in later stages, it can be necessary to also add **backward** edges.

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Code Synthesis

(e₁ e₂)

Chapter 5: Functions

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Ingredients of a Function

The definition of a function consists of

- a name with which it can be called;
- a specification of its formal parameters;
- possibly a result type;
- a sequence of statements.

In C we have:

$\text{code}_{Rf}^i \rho = \text{loadc}_{\underline{f}}^{k_i}$ with \underline{f} starting address of f

Observe:

- function names must have an address assigned to them
- since the size of functions is unknown before they are translated, the addresses of forward-declared functions must be inserted later

int f() { ... }
int g(int f()) { f(); }
g(2f)

loadc k_i F *F: code f ρ*

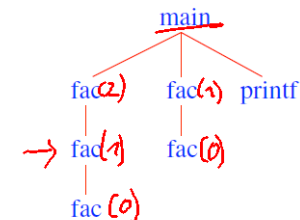
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Memory Management in Functions

```
int fac(int x) {
    if (x <= 0) return 1;
    else return x * fac(x-1);
}
```

```
int main(void) {
    int n;
    n = fac(2) + fac(1);
    printf("%d", n);
}
```

At run-time several instance may be active, that is, the function has been called but has not yet returned.
The recursion tree in the example:



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Memory Management in Function Variables

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- set up a region of memory each time it is called
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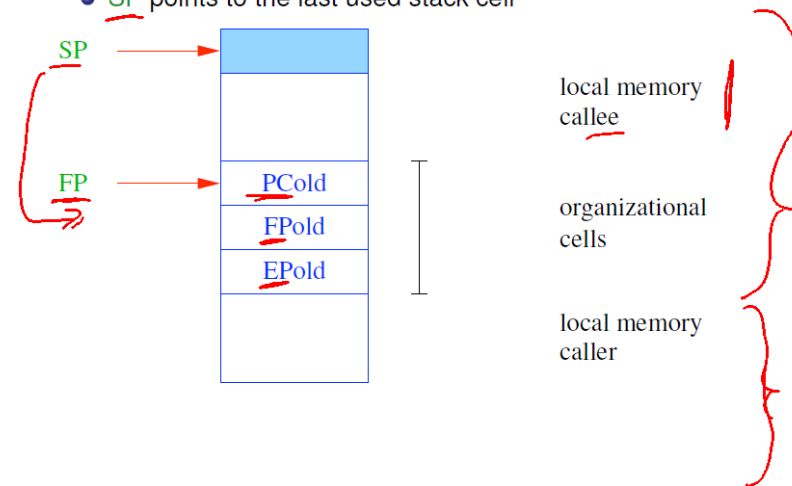
Idea for implementing functions:

- set up a region of memory each time it is called
- in sequential programs this memory region can be allocate on the stack
- thus, each instance of a function has its own region on the stack

3

Organization of a Stack Frame

- stack representation: grows upwards
- SP points to the last used stack cell

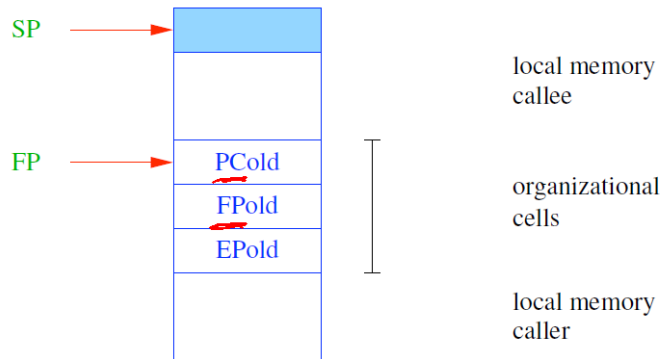


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Organization of a Stack Frame

- stack representation: grows upwards
- SP points to the last used stack cell



- FP $\hat{=}$ frame pointer: points to the last organizational cell
- use to recover the previously active stack frame

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Split of Obligations

Definition

Let f be the current function that calls a function g .

- f is dubbed caller
- g is dubbed callee

The code for managing function calls has to be split between caller and callee.

This split cannot be done arbitrarily since some information is only known in that caller or only in the callee.

Observation:

The space requirement for local parameters is only known by the callee.

Example: `printf(char*s, ...)`

local memory - callee
f(int s) {
char p = malloc(5);*
}

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Principle of Function Call and Return

actions taken on entering g :

- | | | |
|---|--------------------|--------------|
| 1. compute the start address of g | | |
| 2. compute actual parameters | | |
| 3. backup of <u>caller-save registers</u> | } save loc
mark | } are in f |
| 4. backup of <u>FP, EP</u> | | |
| 5. set the new <u>FP</u> | | |
| 6. back up of <u>PC</u> und
jump to the beginning of g | } <u>call</u> | |
| 7. setup new <u>EP</u> | } <u>enter</u> | } are in g |
| 8. allocate <u>space for local variables</u> | } <u>alloc</u> | |

actions taken on leaving g :

- | | | |
|---|----------------------|--------------|
| 1. compute the <u>result</u> | | |
| 2. restore <u>FP, EP, SP</u> | } <u>return</u> | } are in g |
| 3. return to the call site in f ,
that is, restore <u>PC</u> | | |
| 4. restore the <u>caller-save registers</u> | } <u>restore loc</u> | } are in f |
| 5. clean up stack | } <u>pop k</u> | |

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